Package: lsei (via r-universe)

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Title Solving Least Squares or Quadratic Programming Problems under Equality/Inequality Constraints

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Description It contains functions that solve least squares linear regression problems under linear equality/inequality constraints. Functions for solving quadratic programming problems are also available, which transform such problems into least squares ones first. It is developed based on the 'Fortran' program of Lawson and Hanson (1974, 1995), which is public domain and available at <<http://www.netlib.org/lawson-hanson/>>.

Encoding UTF-8

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URL <https://www.stat.auckland.ac.nz/~yongwang/>

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RemoteUrl https://github.com/cran/lsei

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Contents

hfti *Least Squares Solution using Householder Transformation*

Description

Solves the least squares problem using Householder forward triangulation with column interchanges. It is an R interface to the HFTI function that is described in Lawson and Hanson (1974, 1995). Its Fortran implementation is public domain and is available at <http://www.netlib.org/lawson-hanson/>.

Usage

 $hfti(a, b, tol = 1e-07)$

Arguments

Details

Given matrix a and vector b, hfti solves the least squares problem:

minimize $||ax - b||$.

Value

Author(s)

Yong Wang <yongwang@auckland.ac.nz>

References

Lawson and Hanson (1974, 1995). Solving least squares problems. Englewood Cliffs, N.J., Prentice-Hall.

 $\frac{1}{3}$

See Also

[lsei](#page-3-1), [nnls](#page-6-1).

Examples

```
a = matrix(rnorm(10*4), nrow=10)b = a %*% c(0,1,-1,1) + rnorm(10)
hfti(a, b)
```
indx *Index-finding in a Sorted Vector*

Description

For each of given values, indx finds the index of the value in a vector sorted in ascending order that the given value is barely greater than or equal to.

Usage

indx(x, v)

Arguments

Details

For each x[i], the function returns integer j such that

 $v_j \leq x_i < v_{j+1}$

where $v_0 = -\infty$ and $v_{n+1} = \infty$.

Value

Returns a vector of integers, that are indices of x-values in vector v.

Author(s)

Yong Wang <yongwang@auckland.ac.nz>

Examples

indx(0:6,c(1:5,5)) indx(sort(rnorm(5)),-2:2) lsei *Least Squares and Quadratic Programming under Equality and Inequality Constraints*

Description

These functions can be used for solving least squares or quadratic programming problems under general equality and/or inequality constraints.

Usage

```
lsei(a, b, c=NULL, d=NULL, e=NULL, f=NULL, lower=-Inf, upper=Inf)
lsi(a, b, e=NULL, f=NULL, lower=-Inf, upper=Inf)
ldp(e, f)qp(q, p, c=NULL, d=NULL, e=NULL, f=NULL, lower=-Inf, upper=Inf, tol=1e-15)
```
Arguments

Details

The lsei function solves a least squares problem under both equality and inequality constraints. It is an implementation of the LSEI algorithm described in Lawson and Hanson (1974, 1995).

The lsi function solves a least squares problem under inequality constraints. It is an implementation of the LSI algorithm described in Lawson and Hanson (1974, 1995).

The ldp function solves a least distance programming problem under inequality constraints. It is an R wrapper of the LDP function which is in Fortran, as described in Lawson and Hanson (1974, 1995).

lsei 5

The qp function solves a quadratic programming problem, by transforming the problem into a least squares one under the same equality and inequality constraints, which is then solved by function lsei.

The NNLS and LDP Fortran implementations used internally is downloaded from [http://www.](http://www.netlib.org/lawson-hanson/) [netlib.org/lawson-hanson/](http://www.netlib.org/lawson-hanson/).

Given matrices a, c and e, and vectors b, d and f, function lsei solves the least squares problem under both equality and inequality constraints:

```
minimize ||ax - b||,
subject to cx = d, ex \ge f.
```
Function lsi solves the least squares problem under inequality constraints:

```
minimize ||ax - b||,
 subject to ex \geq f.
```
Function ldp solves the least distance programming problem under inequality constraints:

```
minimize ||x||,
subject to ex \geq f.
```
Function qp solves the quadratic programming problem:

minimize
$$
\frac{1}{2}x^T qx + p^T x
$$
,
subject to $cx = d, ex \ge f$.

Value

A vector of the solution values

Author(s)

Yong Wang <yongwang@auckland.ac.nz>

References

Lawson and Hanson (1974, 1995). Solving least squares problems. Englewood Cliffs, N.J., Prentice-Hall.

See Also

[nnls](#page-6-1),[hfti](#page-1-1).

Examples

```
beta = c(rnorm(2), 1)
beta[beta<0] = 0beta = beta / sum(beta)
a = matrix(rnorm(18), ncol=3)b = a %*% beta + rnorm(3, sd=.1)c = t(rep(1, 3))d = 1e = diag(1,3)f = rep(0,3)lsei(a, b) # under no constraint
1sei(a, b, c, d)   # under eq. constraints<br>1sei(a, b, e=e, f=f)   # under ineq. constraints
                                  # under ineq. constraints
lsei(a, b, c, d, e, f) # under eq. and ineq. constraints
lsei(a, b, rep(1,3), 1, lower=0) # same solution
q = crossprod(a)p = -drop(crossprod(b, a))qp(q, p, rep(1,3), 1, lower=0) # same solution
## Example from Lawson and Hanson (1974), p.140
a = \text{cbind}(c(.4302,.6246), c(.3516,.3384))b = c(.6593, .9666)c = c(.4087, .1593)d = .1376lsei(a, b, c, d) # Solution: -1.177499 3.884770
## Example from Lawson and Hanson (1974), p.170
a = \text{cbind}(c(.25,.5,.5,.8), rep(1,4))b = c(.5,.6,.7,1.2)e = \text{cbind}(c(1, 0, -1), c(0, 1, -1))f = c(0, 0, -1)lsi(a, b, e, f) # Solution: 0.6213152 0.3786848
## Example from Lawson and Hanson (1974), p.171:
e = cbind(c(-.207,-.392,.599), c(2.558, -1.351, -1.206))
f = c(-1.3, -.084, .384)ldp(e, f) # Solution: 0.1268538 -0.2554018
```
matMaxs *Row or Column Maximum Values of a Matrix*

Description

Finds either row or column maximum values of a matrix.

Usage

 $mathmaxS(x, \dim = 1)$

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Arguments

Details

Matrix x may contain Inf or -Inf, but not NA or NaN.

Value

Returns a numeric vector with row or column maximum values.

The function is very much the same as using $apply(x, 1, max)$ or $apply(x, 2, max)$, but faster.

Author(s)

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Examples

```
x = \text{cbind}(c(1:4, \text{Inf}), 5:1)matMaxs(x)
matMaxs(x, 2)
```


Description

These functions are particularly useful for solving least squares or quadratic programming problems when some or all of the solution values are subject to nonnegativity constraint. One may further restrict the NN-restricted coefficients to have a fixed positive sum.

Usage

nnls(a, b) pnnls(a, b, k=0, sum=NULL) pnnqp(q, p, k=0, sum=NULL, tol=1e-20)

Arguments

Details

Function nnls solves the least squares problem under nonnegativity (NN) constraints. It is an R interface to the NNLS function that is described in Lawson and Hanson (1974, 1995). Its Fortran implementation is public domain and available at <http://www.netlib.org/lawson-hanson/> (with slight modifications by Yong Wang for compatibility with the lastest Fortran compiler.)

Given matrix a and vector b, nnls solves the nonnegativity least squares problem:

```
minimize ||ax - b||,
 subject to x > 0.
```
Function pnnls also solves the above nonnegativity least squares problem when k=0, but it may also leave the first k coefficients unrestricted. The output value of k can be smaller than the input one, if a has linearly dependent columns. If sum is a positive value, pnnls solves the problem by further restricting that the NN-restricted coefficients must sum to the given value.

Function pnnqp solves the quadratic programming problem

$$
minimize \frac{1}{2}x^Tqx + p^Tx,
$$

when only some or all coefficients are restricted by nonnegativity. The quadratic programming problem is solved by transforming the problem into a least squares one under the same constraints, which is then solved by function pnnls. Arguments k and sum have the same meanings as for pnnls.

Functions nnls, pnnls and pnnqp are able to return any zero-valued solution as 0 exactly. This differs from functions lsei and qp, which may produce very small values for exactly 0s, thanks to numerical errors.

Value

Author(s)

Yong Wang <yongwang@auckland.ac.nz>

References

Lawson and Hanson (1974, 1995). Solving Least Squares Problems. Englewood Cliffs, N.J., Prentice-Hall.

Dax (1990). The smallest point of a polytope. Journal of Optimization Theory and Applications, 64, pp. 429-432.

Wang (2010). Fisher scoring: An interpolation family and its Monte Carlo implementations. Computational Statistics and Data Analysis, 54, pp. 1744-1755.

See Also

[lsei](#page-3-1), [hfti](#page-1-1).

Examples

```
a = matrix(rnorm(40), nrow=10)b = drop(a %*% c(0,1,-1,1)) + rnorm(10)
nnls(a, b)$x # constraint x >= 0
pnnls(a, b, k=0)$x \# same as nnls(a, b)
pnnls(a, b, k=2)$x # first two coeffs are not NN-constrained
pnnls(a, b, k=2, sum=1)$x # NN-constrained coeffs must sum to 1
pnnls(a, b, k=2, sum=2)$x # NN-constrained coeffs must sum to 2
q = crossprod(a)p = -drop(crossprod(b, a))pnnqp(q, p, k=2, sum=2)$x # same solution
pnnls(a, b, sum=1)$x # zeros found exactly
pnnqp(q, p, sum=1)$x # zeros found exactly
lsei(a, b, rep(1,4), 1, lower=0) # zeros not so exact
```
Index

∗ algebra hfti , [2](#page-1-0) indx , [3](#page-2-0) lsei , [4](#page-3-0) matMaxs, [6](#page-5-0) nnls , [7](#page-6-0) ∗ array hfti , [2](#page-1-0) indx , [3](#page-2-0) lsei , [4](#page-3-0) matMaxs , [6](#page-5-0) nnls , [7](#page-6-0) hfti , [2](#page-1-0) , *[5](#page-4-0)* , *[9](#page-8-0)* indx , [3](#page-2-0) ldp *(*lsei *)* , [4](#page-3-0) lsei, [3](#page-2-0), [4](#page-3-0), [9](#page-8-0) lsi *(*lsei *)* , [4](#page-3-0) matMaxs, [6](#page-5-0) nnls , *[3](#page-2-0)* , *[5](#page-4-0)* , [7](#page-6-0) pnnls *(*nnls *)* , [7](#page-6-0) pnnqp *(*nnls *)* , [7](#page-6-0)

qp *(*lsei *)* , [4](#page-3-0)